

# “Evolution of magnetic fields in collapsing star-forming clouds under different environments”

accepted by MNRAS (arXiv:1801.02869)

Star formation during collapsing phase  
in low metallicity environments

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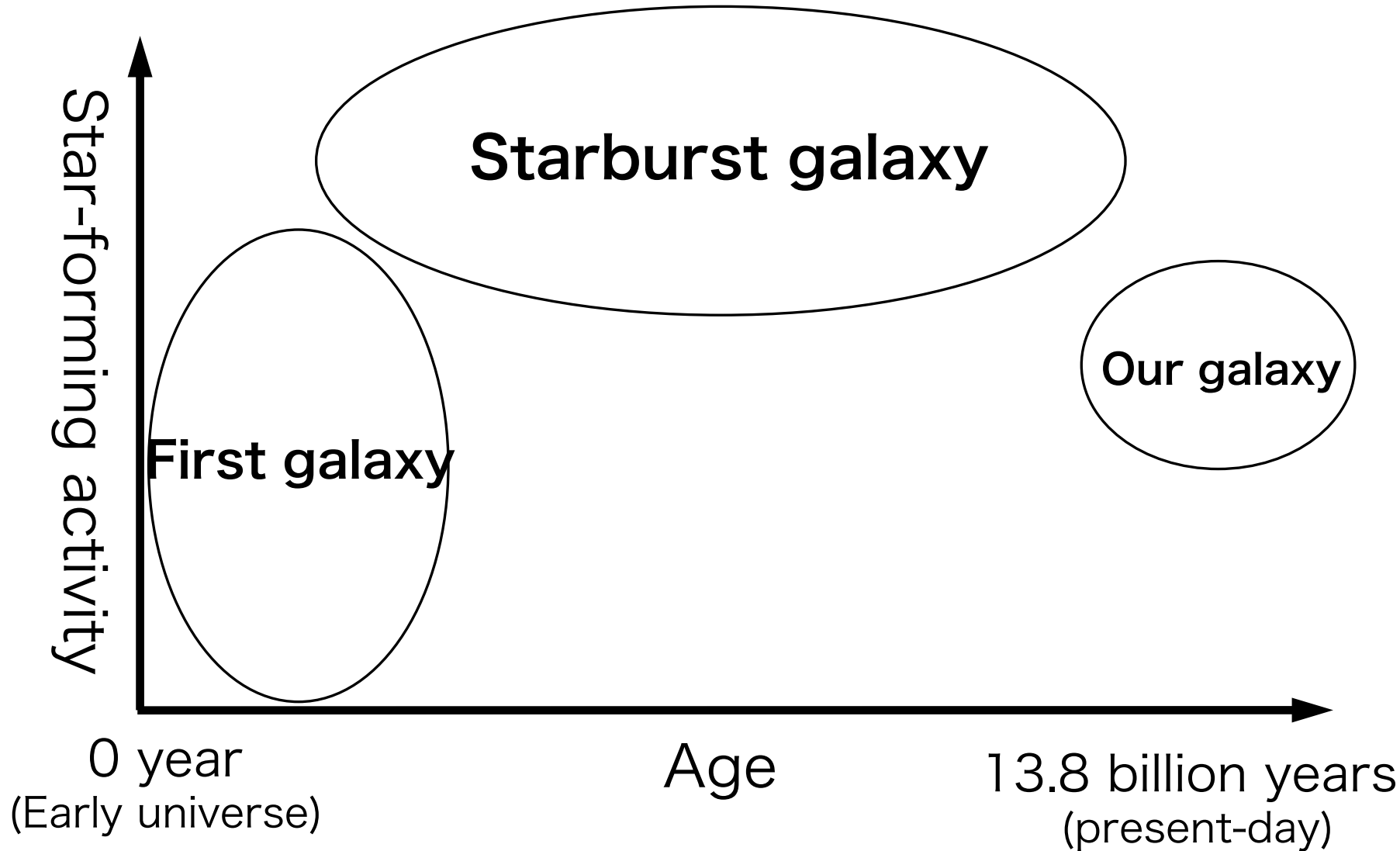
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# Various star-forming environments



# The transition of star formation

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## FIRST STAR

- IMF composed predominantly of high mass stars (Abel+ 02; Bromm+ 02; O'Shea & Norman 07; Yoshida+ 08; Hosokawa+ 11)

## PRESENT-DAY STAR

- IMF composed predominantly of low mass stars (Kroupa 2002; Chabrier 2003)



Where is the transition?

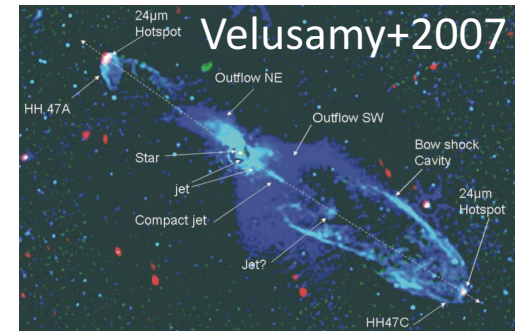
This transition  $Z_{\text{cri}}$  is  $10^{-6} - 10^{-3} Z_{\text{sun}}$  ?

(e.g., Bromm+ 01; Bromm & Loeb 03; Omukai+ 05, 10; Santoro & Shull 06; Frebel+ 07; Dopcke+ 11; Schneider+ 06, 12)

# Outflow during star formation

## ▪ present-day, Our galaxy

- Observation examples (Wu+2004; Zhang+2005)
  - > Theoretical study
  - > Outflow contributes to the star formation



# Models

## INITIAL CONDITIONS

- 28 clouds have each critical Bonner-Ebert density profiles

Ionization parameter  
 $\times$   $C_\zeta = 0, 0.01, 1, 10$   
 Metallicity

$Z/Z_\odot = 0, 10^{-5}, 10^{-4}, 10^{-3}, 10^{-2}, 10^{-1}, 1$

- Magnetic field strength  $B_0$   
( $B$  is adjusted such that  $\mu_0 = 3$ )

- rotation  $\omega (\equiv \Omega_0 t_{\text{ff}}) = 10^{-1}$

$\Omega_0$ : initial angular velocity

$t_{\text{ff}}$ : free-fall time

## BASIC EQUATIONS

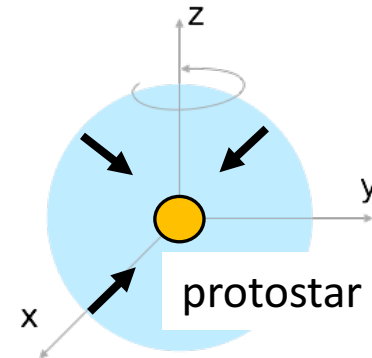
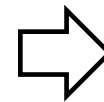
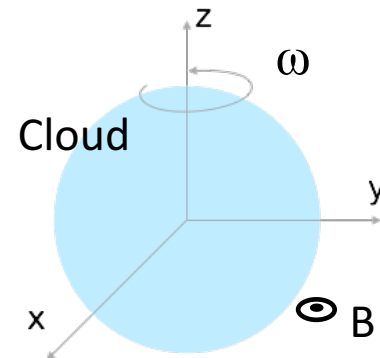
$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\rho \frac{\partial \mathbf{v}}{\partial t} + \rho (\mathbf{v} \cdot \nabla) \mathbf{v} = -\nabla P - \frac{1}{4\pi} \mathbf{B} \times (\nabla \times \mathbf{B}) - \rho \nabla \phi$$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \left[ \mathbf{v} \times \mathbf{B} + \frac{\eta_{\text{AD}}}{|\mathbf{B}|^2} [(\nabla \times \mathbf{B}) \times \mathbf{B}] \times \mathbf{B} - \eta_{\text{OD}} \nabla \times \mathbf{B} \right]$$

$$\nabla^2 \phi = 4\pi G \rho$$

$$P = P(\rho)$$



Ionization rate  $\zeta$        $\zeta = \zeta_{\text{CR}} + \zeta_{\text{RE,short}} + \zeta_{\text{RE,long}}$

▪ **Radioactivity**

- Short-lived REs
- Long-lived REs

$$\zeta_{\text{RE,short}} = 7.6 \times 10^{-19} \text{ s}^{-1} C_{\zeta}$$

$$\zeta_{\text{RE,long}} = 1.4 \times 10^{-22} \text{ s}^{-1} \left( \frac{Z}{Z_{\text{sun}}} \right)$$

▪ **Cosmic rays (CR)**

$$\zeta_{\text{CR}} = C_{\zeta} \zeta_{\text{CR},0} \exp\left(-\frac{\rho R_{\text{J}}}{\lambda}\right)$$

$C_{\zeta}$	Environments
0	Purely primordial environment, no ionization source is included
0.01	Low-metallicity environment, weak ionization sources exist
1	Nearby star-forming environment, the ionization intensity is the same as in nearby star-forming regions ( $\zeta_{\text{CR},0} = 1 \times 10^{-17} \text{ s}^{-1}$ )
10	Starburst galaxy environment: many (or strong) ionization sources exist

$$R_{\text{J}} = \sqrt{\frac{\pi k_{\text{B}} T}{G \mu m_{\text{p}} \rho}}$$

$\lambda$ : attenuation length ( $\lambda = 96 \text{ g cm}^{-2}$ )

$R_{\text{J}}$ : Jeans length

# Initial parameters

	Model	$C_\zeta$	$Z/Z_{\text{sun}}$	$\mu_0$	$B_0(\mu\text{G})$	$\Omega_0(\text{s}^{-1})$	$M_{\text{cl}}(M_\odot)$	$T_{\text{cl}}(\text{K})$	$r_{\text{cl}}(\text{AU})$
1	I0ZPM3		0	3	34.1	$1.31 \times 10^{-14}$	$1.08 \times 10^4$	198	$4.91 \times 10^5$
2	I0Z5M3		$10^{-5}$		33.8	$1.31 \times 10^{-14}$	$1.05 \times 10^4$	194	$4.87 \times 10^5$
3	I0Z4M3		$10^{-4}$		31.9	$1.31 \times 10^{-14}$	$8.75 \times 10^3$	172	$4.59 \times 10^5$
4	I0Z3M3	0	$10^{-3}$		24.6	$1.31 \times 10^{-14}$	$3.98 \times 10^3$	103	$3.52 \times 10^5$
5	I0Z2M3		$10^{-2}$		9.83	$1.35 \times 10^{-14}$	$2.27 \times 10^2$	16.4	$1.33 \times 10^5$
6	I0Z1M3		$10^{-1}$		10.3	$1.62 \times 10^{-14}$	$1.26 \times 10^2$	18.1	$9.67 \times 10^4$
7	I0Z0M3		1		5.76	$1.78 \times 10^{-14}$	15.2	5.65	$4.49 \times 10^4$
8	I001ZPM3		0	3	28.4	$1.31 \times 10^{-14}$	$6.20 \times 10^3$	140	$4.09 \times 10^5$
9	I001Z5M3		$10^{-5}$		25.1	$1.31 \times 10^{-14}$	$6.03 \times 10^3$	136	$4.05 \times 10^5$
10	I001Z4M3		$10^{-4}$		26.2	$1.31 \times 10^{-14}$	$4.88 \times 10^3$	117	$3.77 \times 10^5$
11	I001Z3M3	0.01	$10^{-3}$		20.0	$1.31 \times 10^{-14}$	$2.15 \times 10^3$	68.0	$2.87 \times 10^5$
12	I001Z2M3		$10^{-2}$		9.85	$1.35 \times 10^{-14}$	$2.30 \times 10^2$	16.5	$1.34 \times 10^5$
13	I001Z1M3		$10^{-1}$		10.4	$1.62 \times 10^{-14}$	$1.28 \times 10^2$	18.2	$9.72 \times 10^4$
14	I001Z0M3		1		5.76	$1.78 \times 10^{-14}$	15.2	5.64	$4.49 \times 10^4$
15	I1ZPM3		0	3	12.1	$1.31 \times 10^{-14}$	$4.79 \times 10^2$	24.9	$1.74 \times 10^5$
16	I1Z5M3		$10^{-5}$		12.1	$1.31 \times 10^{-14}$	$4.82 \times 10^2$	25.1	$1.74 \times 10^5$
17	I1Z4M3		$10^{-4}$		12.4	$1.31 \times 10^{-14}$	$5.09 \times 10^2$	26.0	$1.77 \times 10^5$
18	I1Z3M3	1	$10^{-3}$		12.7	$1.31 \times 10^{-14}$	$5.43 \times 10^2$	27.3	$1.81 \times 10^5$
19	I1Z2M3		$10^{-2}$		12.1	$1.34 \times 10^{-14}$	$4.39 \times 10^2$	25.0	$1.66 \times 10^5$
20	I1Z1M3		$10^{-1}$		10.9	$1.59 \times 10^{-14}$	$1.58 \times 10^2$	20.1	$1.06 \times 10^5$
21	I1Z0M3		1		6.11	$1.78 \times 10^{-14}$	18.0	6.34	$4.75 \times 10^4$
22	I10ZPM3		0	3	13.5	$1.31 \times 10^{-14}$	$6.56 \times 10^2$	31.0	$1.93 \times 10^5$
23	I10Z5M3		$10^{-5}$		13.6	$1.31 \times 10^{-14}$	$6.64 \times 10^2$	31.2	$1.94 \times 10^5$
24	I10Z4M3		$10^{-4}$		14.0	$1.32 \times 10^{-14}$	$7.25 \times 10^2$	33.1	$1.99 \times 10^5$
25	I10Z3M3	10	$10^{-3}$		15.3	$1.32 \times 10^{-14}$	$9.39 \times 10^2$	39.6	$2.17 \times 10^5$
26	I10Z2M3		$10^{-2}$		15.3	$1.34 \times 10^{-14}$	$8.67 \times 10^2$	39.6	$2.09 \times 10^5$
27	I10Z1M3		$10^{-1}$		12.6	$1.55 \times 10^{-14}$	$2.74 \times 10^2$	26.8	$1.29 \times 10^5$
28	I10Z0M3		1		8.03	$1.78 \times 10^{-14}$	40.1	11.0	$6.24 \times 10^4$

$$\omega_0 = 10^{-1}$$

$$\alpha_0 \left( \equiv \frac{E_t}{E_g} \right) = 0.47$$

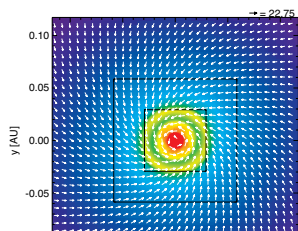
$$\beta_0 \left( \equiv \frac{E_{\text{rot}}}{E_g} \right) = 1.84 \times 10^{-2}$$

# Result: star formation

Present-day star formation  
(has  $Z/Z_{\text{sun}} \sim 1$ )

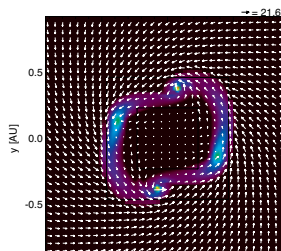
Lower metallicity star formation  
(has  $Z/Z_{\text{sun}} < 10^{-3}$ )

First star  
( $Z/Z_{\text{sun}} = 0$ )



Single star  
(or Massive close binary)

Lower metallicity star



Multiple stars

全く異なる星形成

過程を経る  
(no outflow)

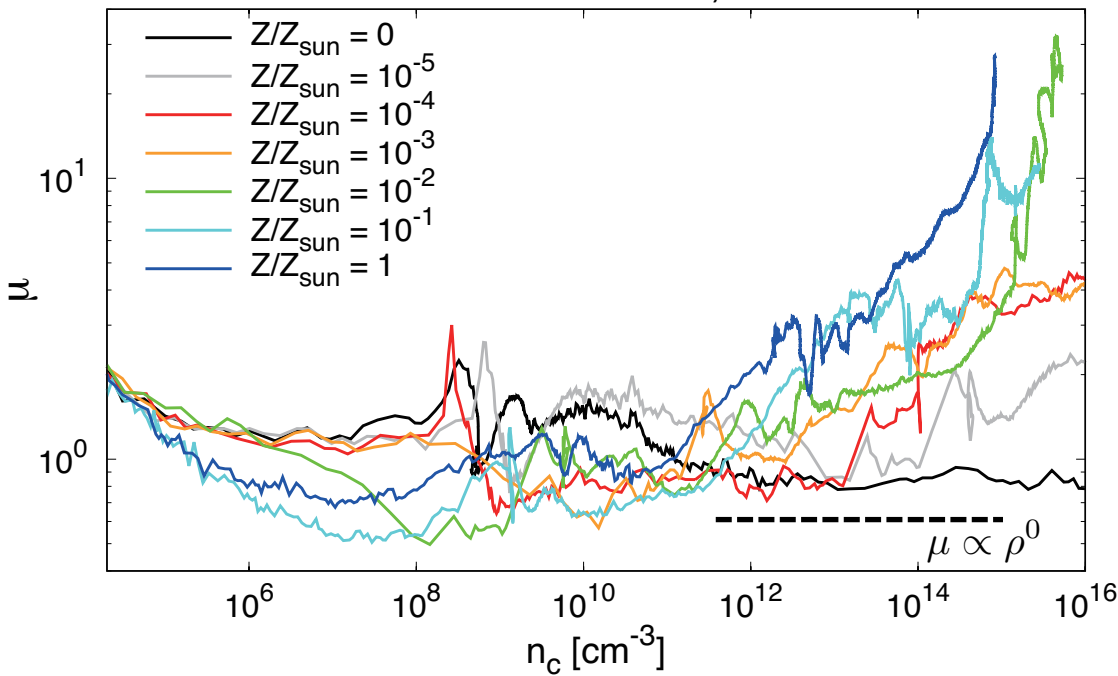


# Mass-to-flux ratio evolution: Comparison of metallicities

Definition

$$\mu_0 = \frac{(M/\Phi)}{(M/\Phi)_{\text{cri}}}, \quad \left(\frac{M}{\Phi}\right)_{\text{cri}} = \frac{1}{2\pi G^{1/2}}.$$

present-day ( $C_\zeta=1$ )



approximation of the mass-to-flux ratio

Case of disk-like collapse

$$\mu \approx \frac{M}{BL^2} \begin{cases} R_J \propto \rho^{(\gamma-2)/2} \\ M_J \propto \rho^{(3\gamma-4)/2} \\ B \propto \rho^{(2\gamma-1)/2} \end{cases}$$

Adopting  $\gamma \sim 1$ ,  $\mu \propto \rho^0$

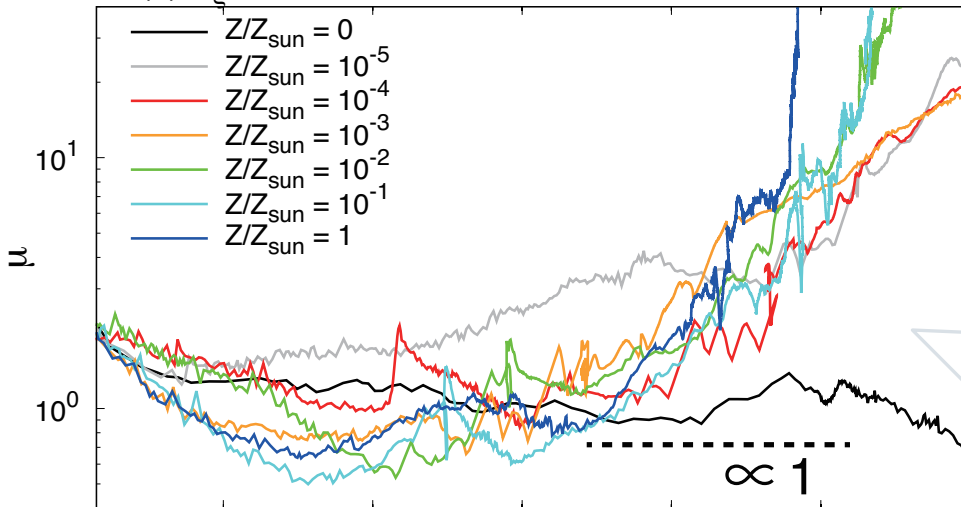
$Z/Z_{\text{sun}} \geq 10^{-5}$

->  $\mu$  value is high

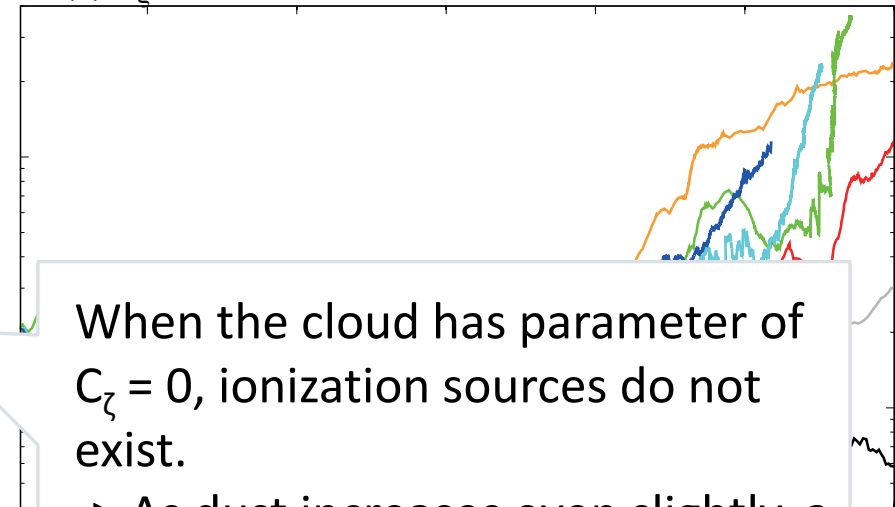
(the magnetic dissipation becomes)

# Mass-to-flux ratio evolution: Comparison of metallicities

(a)  $C_\zeta = 0$



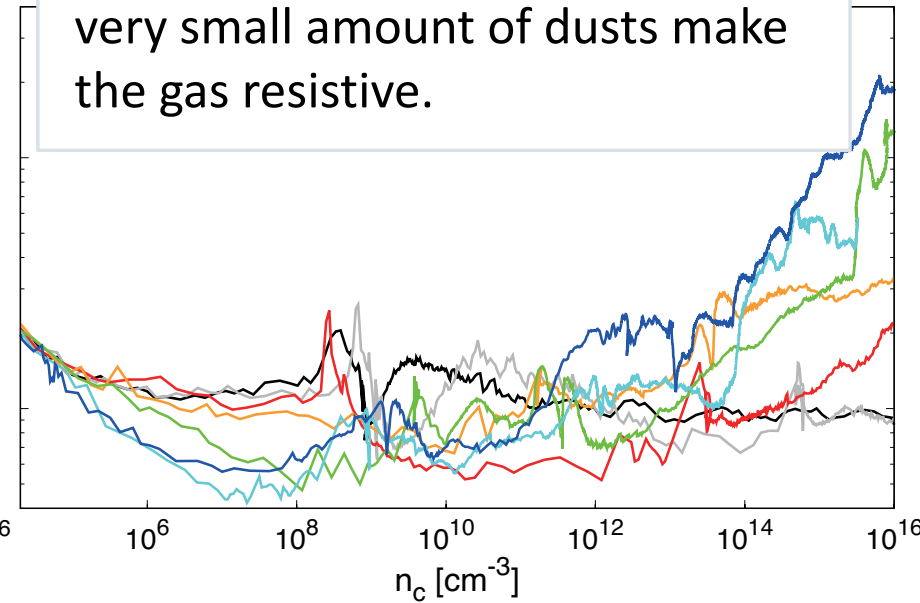
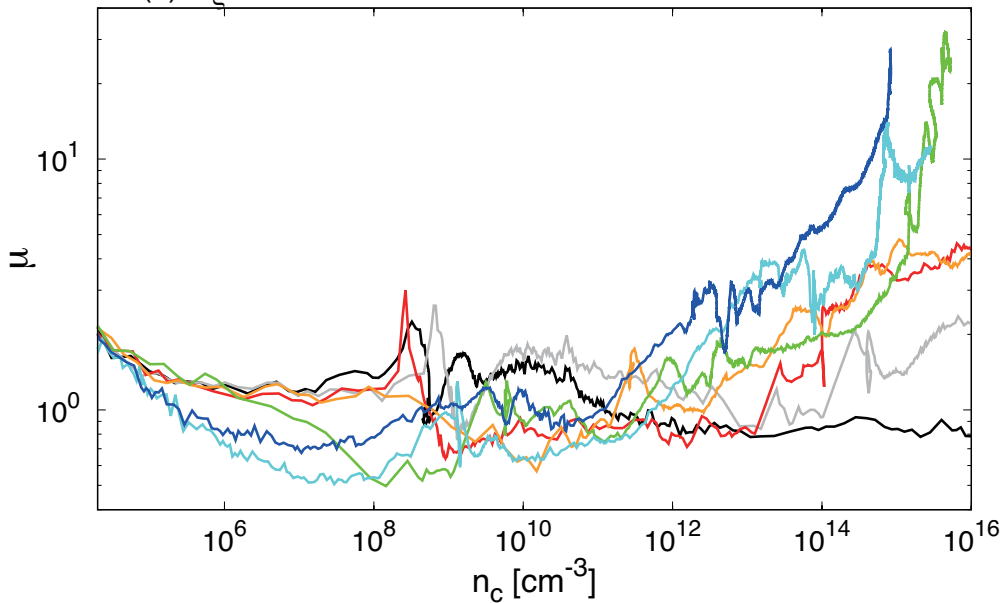
(b)  $C_\zeta = 0.01$



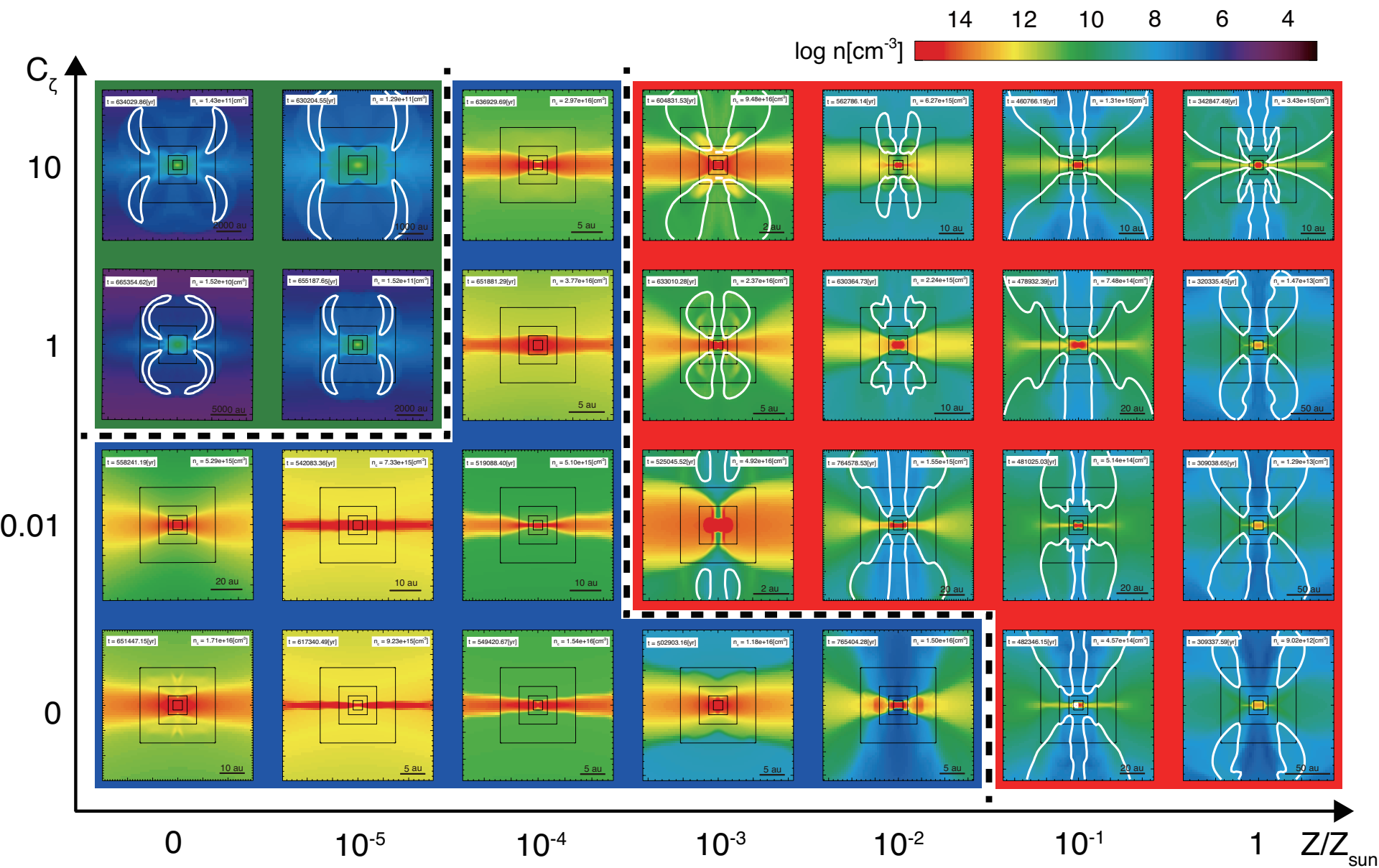
When the cloud has parameter of  $C_\zeta = 0$ , ionization sources do not exist.

-> As dust increases even slightly, a very small amount of dusts make the gas resistive.

(c)  $C_\zeta = 1$



# Driving or not outflow in different environments



# Magnetic field evolution on the $n_c - B$ plane

**magnetic Reynolds number**

$$R_m \equiv v_f \lambda_J \eta^{-1},$$

$$\lambda_J \equiv (\pi c_s^2 / G \rho_c)^{1/2}$$

$$v_f \equiv [(4/3)\pi G \lambda_J^2 \rho_c]^{1/2}$$

$$\eta = \max(\eta_{OD}, \eta_{AD}).$$

**critical magnetic field strength**

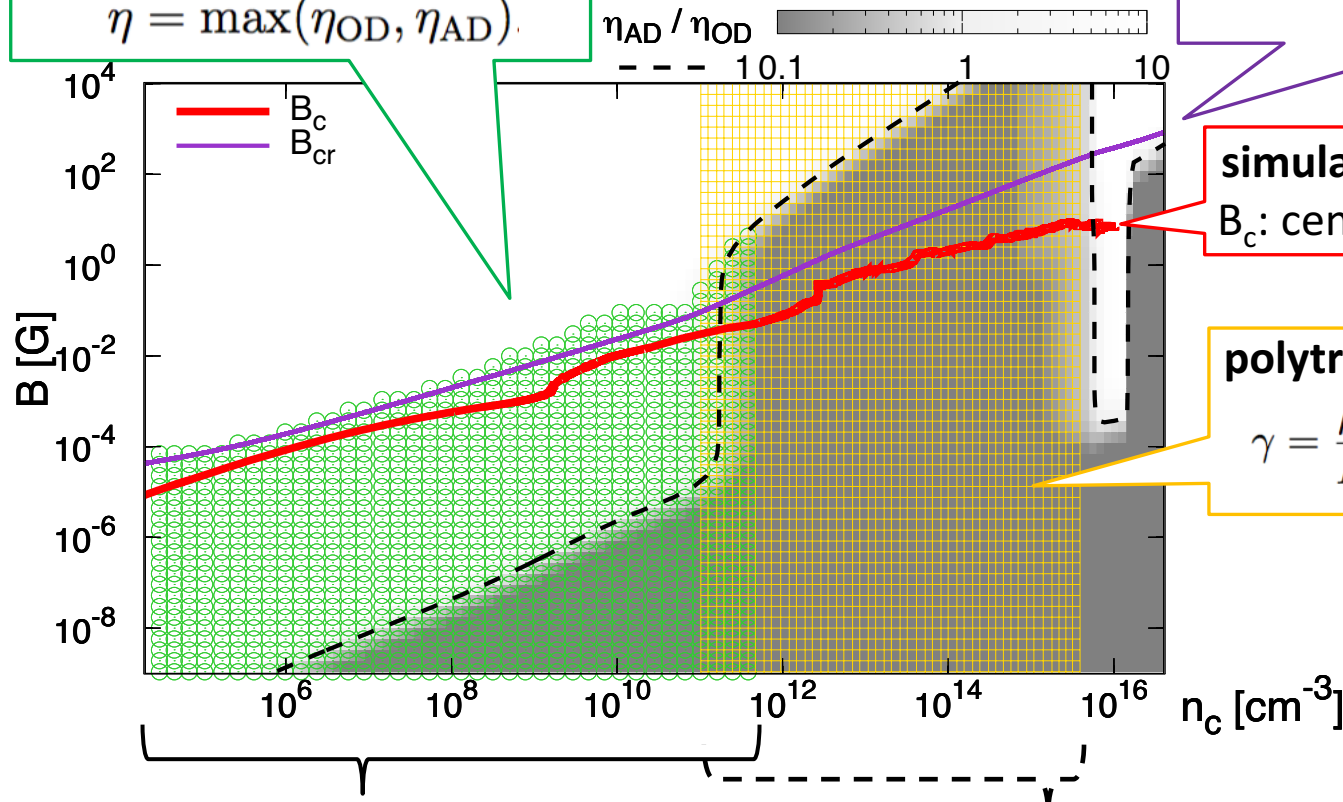
$$B_{cr} = \left( \frac{16\pi^2 G \rho_c^2 \lambda_J^2}{3} \right)^{1/2}$$

**simulation result**

$B_c$ : central magnetic field strength

**polytropic index**

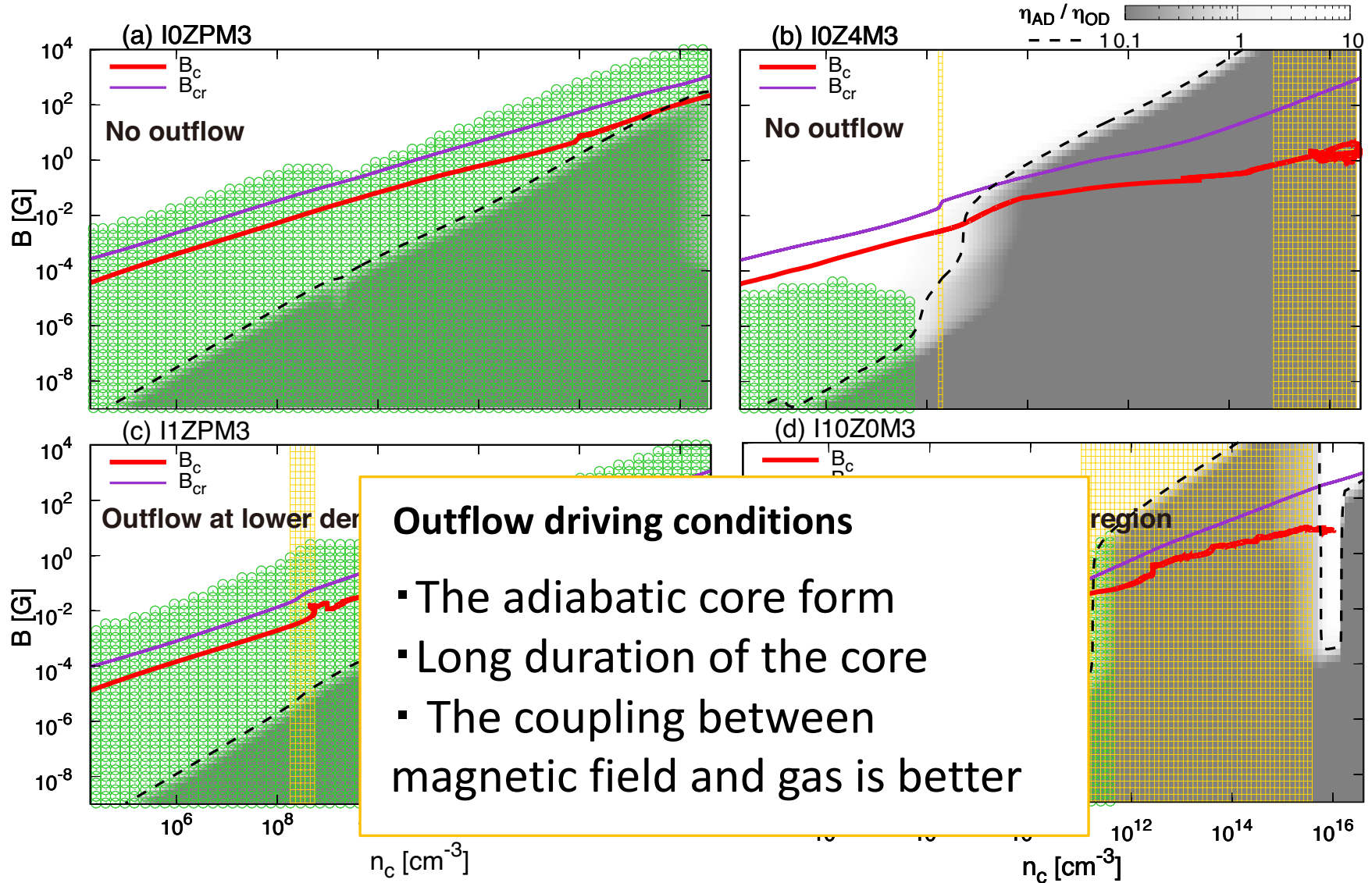
$$\gamma = \frac{\rho_c}{P_c} \left( \frac{dP}{d\rho} \right)_c$$



magnetic field is coupled to the gas ( $R_m > 1$ )

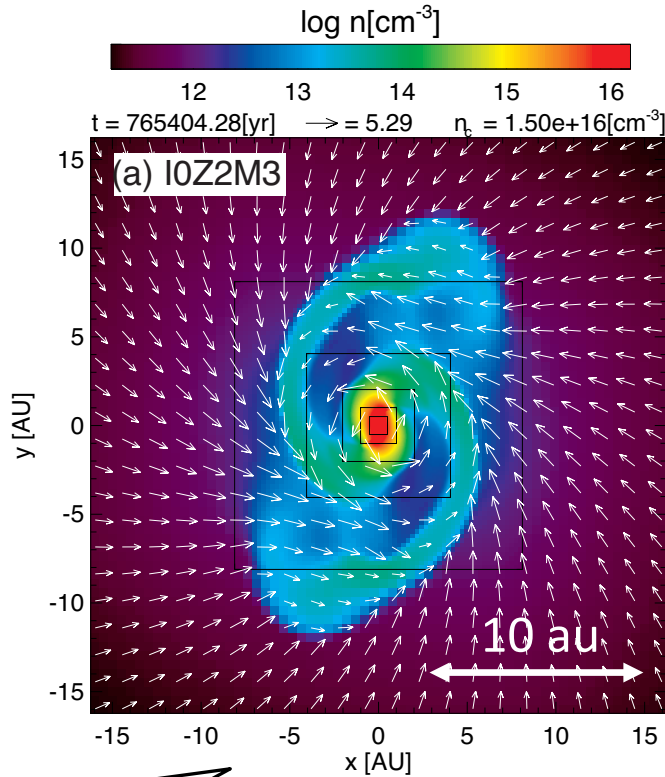
quasi-hydrostatic core can be formed ( $\gamma > 4/3$ )

# Magnetic field evolution on the $n_c - B$ plane



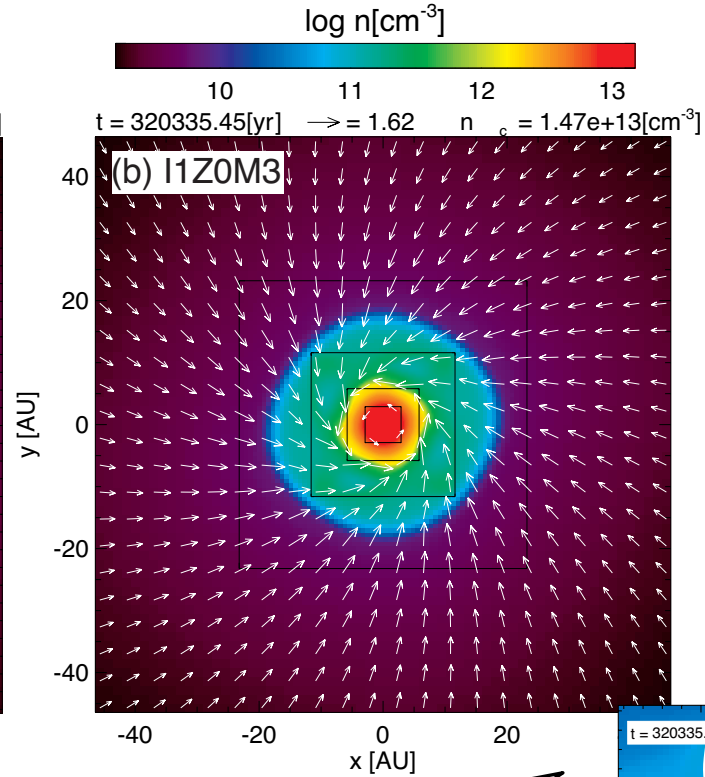
# Angular momentum transfer

Outflow is not driven

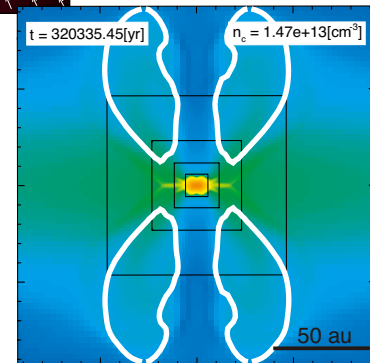


Formation of non-axisymmetric structure of first core scale  
-> Angular momentum is transported by gravity torque

Outflow is driven



Angular momentum is transported by outflow



# Summary

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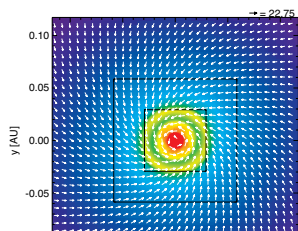
- In the present conditions ( $\mu_0 = 3$ ,  $\omega_0 = 10^{-1}$ ), outflow does not drive in the metallicity range  $Z/Z_{\text{sun}} < 10^{-3}$  expect  $C_\zeta = 1, 10$
- For the case in which  $C_\zeta = 0$  and lower metallicities, star formation process is quite different.
- The transition of star formation exist at  $Z \sim 10^{-4} - 10^{-3} Z_{\text{sun}}$ .

# Result: star formation

Present-day star formation  
(has  $Z/Z_{\text{sun}} \sim 1$ )

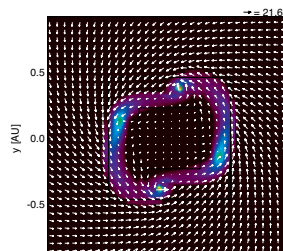
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